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Data-driven parameterized modeling of LTI systems with guaranteed stability

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We consider the problem of extracting a parameterized reduced-order model from a set of measurements of some underlying LTI system with (unknown) transfer function $\check{H}(s; \vartheta) \in \mathbb{C}^{P \times P}$, where s is the Laplace variable and $\vartheta \in \Theta \subset \mathbb{R}^\rho$ is a vector of external parameters. The model is constructed using a data-driven approach starting from frequency response samples $\check{H}_{k,m} = \check{H}(j\omega_k; \vartheta_m)$ at discrete frequency $s_k = j\omega_k$ and parameter values ϑ_m for $k = 1, \dots, \bar{k}$ and $m = 1, \dots, \bar{m}$.

We adopt a Generalized Sanathanan-Koerner (GSK) framework [3] by representing the model as

$$H(s; \vartheta) = \frac{N(s, \vartheta)}{D(s, \vartheta)} = \frac{\sum_{n=0}^{\bar{n}} \sum_{\ell=1}^{\bar{\ell}} R_{n,\ell} \xi_\ell(\vartheta) \varphi_n(s)}{\sum_{n=0}^{\bar{n}} \sum_{\ell=1}^{\bar{\ell}} r_{n,\ell} \xi_\ell(\vartheta) \varphi_n(s)}, \quad (1)$$

where $R_{n,\ell} \in \mathbb{R}^{P \times P}$ and $r_{n,\ell} \in \mathbb{R}$ are the model coefficients, and where $\varphi_n(s)$, $\xi_\ell(\vartheta)$ are suitable basis functions. In particular, we use partial fractions $\varphi_n(s) = (s - q_n)^{-1}$ associated to a set of predetermined stable poles q_n (as in the well-known Vector Fitting scheme [2]) and tensor products of Chebychev polynomials $\xi_\ell(\vartheta)$ for frequency and parameter dependence, respectively. Model coefficients are computed through a Sanathanan-Koerner iteration [3] by setting $D^0(j\omega, \vartheta) = 1$ and solving

$$\min_{k,m} \sum_{k,m} |D^{\mu-1}(j\omega_k, \vartheta_m)|^{-1} \|N^\mu(j\omega_k, \vartheta_m) - D^\mu(j\omega_k, \vartheta_m) \check{H}_{k,m}\|_F^2 \quad \text{for } \mu = 1, 2, \dots \quad (2)$$

Our main result is a sufficient condition and an associated algorithm for enforcing uniform stability of the model $H(s; \vartheta)$ throughout the parameter domain $\vartheta \in \Theta$. This condition requires constraining the model denominator $D(s, \vartheta)$ to be a Positive Real (PR) function (see [1] for the sketch of a proof).

Based on the model structure (1), the PR-ness of $D(s, \vartheta)$ is guaranteed when $\Re\{D(j\omega, \vartheta)\} \geq 0, \forall \vartheta \in \Theta$ and $\forall \omega \in \mathbb{R}$. This is achieved by an adaptive sampling process in the parameter space Θ . At GSK iteration μ and for any given ϑ_* , the imaginary eigenvalues of the Hamiltonian matrix associated to a state-space realization of $D^{\mu-1}$ are used to determine the frequency bands where $\Re\{D^{\mu-1}(j\omega, \vartheta_*)\} < 0$, and a first-order perturbation analysis of the non-imaginary Hamiltonian eigenvalues is used to determine which directions need to be searched in the parameter space to find local minima of $\Re\{D^{\mu-1}\}$. The result is an automatically determined set of discrete points (ω_i, ϑ_i) where the constraint $\Re\{D^\mu(j\omega_i, \vartheta_i)\} > 0$ is formulated and embedded in the GSK iteration (2). When the residual of (2) stabilizes, the model poles $p_n(\vartheta)$ (i.e., the zeros of $D(s, \vartheta)$) result uniformly stable $\forall \vartheta \in \Theta$.

Several examples from Electronic Design Automation applications are provided, demonstrating the robustness and the efficiency of proposed approach. For a preview of these examples, see [1].

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